

$$8\cos^4 x = 11\cos 2x - 1$$

$$\cos 2x = 2\cos^2 x - 1$$

$$\cos^2 x = (\cos 2x + 1)/2$$

$$8(\cos^2 x)^2 = 11\cos 2x - 1$$

$$8((\cos 2x + 1)/2)^2 = 11\cos 2x - 1$$

$$2(\cos^2 2x + 2\cos 2x + 1) = 11\cos 2x - 1$$

$$\cos 2x = t$$

$$2(t^2 + 2t + 1) = 11t - 1$$

$$2t^2 + 4t + 2 = 11t - 1$$

$$2t^2 - 7t + 3 = 0$$

$$D = 49 - 24 = 25$$

$$t_1 = (7 + 5)/4 = 3$$

$$t_2 = (7 - 5)/4 = 1/2$$

$$\cos 2x = 3 \text{ Нельзя}$$

$$\cos 2x = 1/2$$

$$2x = \pi/3 + 2\pi n$$

$$x = \pi/6 + \pi n$$

$$2x = 5\pi/3 + 2\pi n$$

$$x = 5\pi/6 + \pi n$$

$$\text{Ответ: } \pi/6 + \pi n; 5\pi/6 + \pi n$$

$$\sin^4 x + \cos^4 x = \sin x \cos x$$

$$\cos^2 x = (\cos 2x + 1)/2$$

$$\sin^4 x + (\cos^2 x)^2 = \sin x \cos x$$

$$\sin^4 x + ((\cos 2x + 1)/2)^2 = \sin x \cos x$$

$$\sin^4 x + (\cos 2x + 1)^2/4 = \sin x \cos x \quad | \cdot 4$$

$$4\sin^4 x + (\cos 2x + 1)^2 = 4\sin x \cos x$$

$$\sin 2x = 2 \sin x \cos x$$

$$4\sin^4 x + \cos^2 2x + 2 \cos 2x + 1 = 2 \sin 2x$$

$$\sin^2 x = (1 - \cos 2x)/2$$

$$4(\sin^2 x)^2 + \cos^2 2x + 2 \cos 2x + 1 = 2 \sin 2x$$

$$4((1 - \cos 2x)/2)^2 + \cos^2 2x + 2 \cos 2x + 1 = 2 \sin 2x$$

$$4(1 - \cos 2x)^2/4 + \cos^2 2x + 2 \cos 2x + 1 = 2 \sin 2x$$

$$(1 - \cos 2x)^2 + \cos^2 2x + 2 \cos 2x + 1 = 2 \sin 2x$$

$$\cos^2 2x - 2 \cos 2x + 1 + \cos^2 2x + 2 \cos 2x + 1 = 2 \sin 2x$$

$$2\cos^2 2x + 2 = 2 \sin 2x \quad | :2$$

$$\cos^2 2x + 1 = \sin 2x$$

$$\cos^2 2x = 1 - \sin^2 2x$$

$$1 - \sin^2 2x + 1 = \sin 2x$$

$$\sin^2 2x + \sin 2x - 2 = 0$$

$$\sin 2x = t$$

$$t^2 + t - 2 = 0$$

$$t_1 = -2$$

$$t_2 = 1$$

$$\sin 2x = 1$$

$$2x = \pi/2 + 2\pi n$$

$$x = \pi/4 + \pi n$$

$$\text{Ответ: } \pi/4 + \pi n$$

$$\sin^4 x + \cos^4 x = \sin x \cos x$$

$$\sin^4 x + 2 \sin^2 x \cos^2 x + \cos^4 x = \sin x \cos x + 2 \sin^2 x \cos^2 x$$

$$(\sin^2 x + \cos^2 x)^2 = \sin x \cos x (1 + 2 \sin x \cos x)$$

$$1 = \sin x \cos x (1 + 2 \sin x \cos x)$$

$$\sin x \cos x = t$$

$$1 = t(1 + 2t)$$

$$1 = t + 2t^2$$

$$2t^2 + t - 1 = 0$$

$$D = 1 + 8 = 9$$

$$t_1 = (-1 + 3)/4 = 1/2$$

$$t_2 = (-1 - 3)/4 = -1$$

$$\sin x \cos x = 1/2 \quad | \cdot 2$$

$$2 \sin x \cos x = 1$$

$$\sin 2x = 1$$

$$2x = \pi/2 + 2\pi n$$

$$x = \pi/4 + \pi n$$

$$\sin x \cos x = -1 \quad | \cdot 2$$

$$2 \sin x \cos x = -2$$

$$\sin 2x = -2$$

$$\text{Ответ: } \pi/4 + \pi n$$